

## Lesson 17: Equations Involving Factored Expressions

### Classwork

#### Exercise 1

1. Solve each equation for  $x$ .

a.  $x - 10 = 0$

b.  $\frac{x}{2} + 20 = 0$

c. Demanding Dwight insists that you give him two solutions to the following equation:

$$(x - 10)\left(\frac{x}{2} + 20\right) = 0$$

Can you provide him with two solutions?

d. Demanding Dwight now wants FIVE solutions to the following equation:

$$(x - 10)(2x + 6)(x^2 - 36)(x^2 + 10)\left(\frac{x}{2} + 20\right) = 0$$

Can you provide him with five solutions?

Do you think there might be a sixth solution?

Consider the equation  $(x - 4)(x + 3) = 0$ .

e. Rewrite the equation as a compound statement.

f. Find the two solutions to the equation.

### Example 1

Solve  $2x^2 - 10x = 0$ , for  $x$ .

### Example 2

Solve  $x(x - 3) + 5(x - 3) = 0$ , for  $x$ .

### Exercises 2–7

2.  $(x + 1)(x + 2) = 0$

3.  $(3x - 2)(x + 12) = 0$

4.  $(x - 3)(x - 3) = 0$

5.  $(x + 4)(x - 6)(x - 10) = 0$

6.  $x^2 - 6x = 0$

7.  $x(x - 5) + 4(x - 5) = 0$

**Example 3**

Consider the equation  $(x - 2)(2x - 3) = (x - 2)(x + 5)$ . Lulu chooses to multiply through by  $\frac{1}{x-2}$  and gets the answer  $x = 8$ . But Poindexter points out that  $x = 2$  is also an answer, which Lulu missed.

a. What's the problem with Lulu's approach?

b. Use factoring to solve the original equation for  $x$ .

**Exercises 8–11**

8. Use factoring to solve the equation for  $x$ :  $(x - 2)(2x - 3) = (x - 2)(x + 1)$ .

9. Solve each of the following for  $x$ :

a.  $x + 2 = 5$

b.  $x^2 + 2x = 5x$

c.  $x(5x - 20) + 2(5x - 20) = 5(5x - 20)$

10.

a. Verify:  $(a - 5)(a + 5) = a^2 - 25$ .

b. Verify:  $(x - 88)(x + 88) = x^2 - 88^2$ .

c. Verify:  $A^2 - B^2 = (A - B)(A + B)$ .

d. Solve for  $x$ :  $x^2 - 9 = 5(x - 3)$ .

e. Solve for  $w$ :  $(w + 2)(w - 5) = w^2 - 4$ .

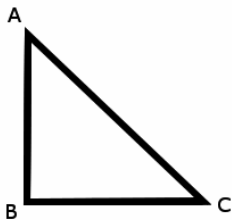
11. A string 60 inches long is to be laid out on a tabletop to make a rectangle of perimeter 60 inches. Write the width of the rectangle as  $15 + x$  inches. What is an expression for its length? What is an expression for its area? What value for  $x$  gives an area of the largest possible value? Describe the shape of the rectangle for this special value of  $x$ .

**Lesson Summary**

The *zero-product property* says that if  $ab = 0$ , then either  $a = 0$  or  $b = 0$  or  $a = b = 0$ .

**Problem Set**

- Find the solution set of each equation:
  - $(x - 1)(x - 2)(x - 3) = 0$
  - $(x - 16.5)(x - 109) = 0$
  - $x(x + 7) + 5(x + 7) = 0$
  - $x^2 + 8x + 15 = 0$
  - $(x - 3)(x + 3) = 8x$
- Solve  $x^2 - 11x = 0$ , for  $x$ .
- Solve  $(p + 3)(p - 5) = 2(p + 3)$ , for  $p$ . What solution do you lose if you simply divide by  $p + 3$  to get  $p - 5 = 2$ ?
- The square of a number plus 3 times the number is equal to 4. What is the number?
- In the right triangle shown below, the length of side AB is  $x$ , the length of side BC is  $x + 2$ , and the length of the hypotenuse AC is  $x + 4$ . Use this information to find the length of each side. (Use the Pythagorean theorem to get an equation, and solve for  $x$ .)



- Using what you learned in this lesson, create an equation that has 53 and 22 as its only solutions.