Name	Date	

- 1. The number of users of social media has increased significantly since the year 2001. In fact, the approximate number of users has tripled each year. It was reported that in 2005 there were 3 million users of social media.
 - Assuming that the number of users continues to triple each year, for the next three years, determine the number of users in 2006, 2007, and 2008.

b. Assume the trend in the numbers of users tripling each year was true for all years from 2001 to 2009. Complete the table below using 2005 as year 1 with 3 million as the number of users that year.

Year	-3	-2	-1	0	1	2	3	4	5
# of									
users in					3				
millions									

c. Given only the number of users in 2005 and the assumption that the number of users triples each year, how did you determine the number of users for years 2, 3, 4, and 5?

d. Given only the number of users in 2005 and the assumption that the number of users triples each year, how did you determine the number of users for years 0, -1, -2, and -3?

Module 1:



e. Write an equation to represent the number of users in millions, N, for year $t, t \ge -3$.

f. Using the context of the problem, explain whether or not the formula $N=3^t$ would work for finding the number of users in millions in year t, for all $t \le 0$.

g. Assume the total number of users continues to triple each year after 2009. Determine the number of users in 2012. Given that the world population at the end of 2011 was approximately 7 billion, is this assumption reasonable? Explain your reasoning.

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- 2. Let *m* be a whole number.
 - a. Use the properties of exponents to write an equivalent expression that is a product of unique primes, each raised to an integer power.

$$\frac{6^{21} \cdot 10^7}{30^7}$$

b. Use the properties of exponents to prove the following identity:

$$\frac{6^{3m} \cdot 10^m}{30^m} = 2^{3m} \cdot 3^{2m}$$

c. What value of m could be substituted into the identity in part (b) to find the answer to part (a)?

Module 1: In



3.

a. Jill writes $2^3 \cdot 4^3 = 8^6$ and the teacher marked it wrong. Explain Jill's error.

b. Find n so that the number sentence below is true:

$$2^3 \cdot 4^3 = 2^3 \cdot 2^n = 2^9$$

c. Use the definition of exponential notation to demonstrate why $2^3 \cdot 4^3 = 2^9$ is true.



Module 1:



d. You write $7^5 \cdot 7^{-9} = 7^{-4}$. Keisha challenges you, "Prove it!" Show directly why your answer is correct without referencing the laws of exponents for integers; in other words, $x^a \cdot x^b = x^{a+b}$ for positive numbers x and integers a and b.



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A Pro	A Progression Toward Mastery							
Assessment Task Item		STEP 1 Missing or incorrect answer and little evidence of reasoning or application of mathematics to solve the problem.	STEP 2 Missing or incorrect answer but evidence of some reasoning or application of mathematics to solve the problem.	STEP 3 A correct answer with some evidence of reasoning or application of mathematics to solve the problem, OR an incorrect answer with substantial evidence of solid reasoning or application of mathematics to solve the problem.	A correct answer supported by substantial evidence of solid reasoning or application of mathematics to solve the problem.			
1	a-d 8.EE.A.1	Student answers 0–1 parts of (a)–(d) correctly. Student is able to complete the table for at least values of 0–5 for part (b). Student is unable to respond to questions or left items blank.	Student answers 2–3 parts of (a)–(d) correctly. Student is able to complete the table in part (b) correctly for 5 or more entries, including at least one value on each side of the value given for year 1. Student provides a limited expression of reasoning in parts (c) and (d).	Student answers 3–4 parts of (a)–(d) correctly. Student provides correct answers with some reasoning for making calculations. OR Student has a few miscalculations but provides substantial reasoning with proper use of grade-level vocabulary.	Student answers all parts of (a)–(d) correctly. Student provides solid reasoning for making calculations with proper use of grade-level vocabulary.			
	e-g 8.EE.A.1	Student answers 0–1 parts of (e)–(g) correctly. Student is unable to relate the pattern in the problem to exponential growth.	Student answers 1–2 parts of (e)–(g) correctly. Student is able to relate the pattern in the problem to exponential growth by writing an equation. Student justifications are incomplete.	Student answers 2–3 parts of (e)–(g) correctly. Equation given is correct, and student is able to answer questions, but justifications are incomplete. OR The equation given relates the pattern to exponential growth but is incomplete or contains a minor error, and student is able to answer questions using solid reasoning based on the information provided.	Student answers all parts of (e)–(g) correctly. Student justifies answers and makes accurate conclusions based on the information provided in the problem. Student is able to explain limitations of the equation when looking ahead in time and back in time.			





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2	8.EE.A.1	Student answers incorrectly. No evidence of use of properties of exponents.	Student answers incorrectly. Properties of exponents are used incorrectly.	Student answers correctly. Some evidence of use of properties of exponents is shown in calculations.	Student answers correctly. Student provides substantial evidence of the use of properties of exponents to simplify the expression to distinct primes.	
	b-c 8.EE.A.1	Student answers parts (b)–(c) incorrectly. No evidence of use of properties of exponents.	Student answers parts (b)–(c) incorrectly. Properties of exponents are used incorrectly.	Student answers part (b) and/or part (c) correctly. Some evidence of use of properties of exponents is shown in calculations.	Student answers both parts (b) and (c) correctly. Student provides substantial evidence of the use of properties of exponents to prove the identity.	
3	8.EE.A.1	Student states that Jill's response is correct. OR Student is unable to identify the mistake and provides no additional information.	Student states that Jill's answer is incorrect. Student is unable to identify the mistake of multiplying unlike bases. Student may have used what he or she knows about exponential notation to multiply numbers to show the answer was incorrect.	Student identifies Jill's error as "multiplied unlike bases."	Student identifies Jill's error as "multiplied unlike bases." Student provides a thorough explanation as to how unlike bases can be rewritten so that properties of exponents can be used properly.	
	b 8.EE.A.1	Student is unable to identify the correct value for <i>n</i> .	Student correctly answers $n=6$. No explanation is provided as to why the answer is correct.	Student correctly answers $n=6$. Student states that $4^3=2^6$ with little or no explanation or work shown.	Student correctly answers $n=6$. Student <i>clearly shows</i> that 4^3 is equivalent to 2^6 .	
	c 8.EE.A.1	Student uses the definition of exponential notation to rewrite 4^3 as $4 \times 4 \times 4$. Student is unable to complete the problem.	Student multiplies 4 ³ to get 64 and is able to rewrite it as a number with a base of 2 but has the wrong exponent.	Student correctly rewrites 4^3 as 2^6 and then uses the first property of exponents to show that the answer is correct.	Student correctly rewrites 4 ³ as 2 ⁶ . Student uses definition of exponential notation to rewrite each number as repeated multiplication. Student clearly shows how/why the exponents are added to simplify such expressions.	





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	d 8.EE.A.1	Student may be able to rewrite 7^{-9} as a fraction but is unable to operate with fractions.	Student is unable to show why part (d) is correct but uses a property of exponents to state that the given answer is correct.	Student answers part (d) but misuses or leaves out definitions in explanations and proofs.	Student answers part (d) correctly and uses definitions and properties to thoroughly explain and prove the answer. Answer shows strong evidence that student understands exponential notation and can use the properties of exponents proficiently.
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Name	Date

- 1. The number of users of social media has increased significantly since the year 2001. In fact, the approximate number of users has tripled each year. It was reported that in 2005 there were 3 million users of social media.
 - a. Assuming that the number of users continues to triple each year, for the next three years, determine the number of users in 2006, 2007, and 2008.

b. Assume the trend in the numbers of users tripling each year was true for all years from 2001 to 2009. Complete the table below using 2005 as year 1 with 3 million as the number of users that year.

r					r				·	
	Year	-3	-2	-1	0	1	2	3	4	5
	# of users in millions	177	4	13	1	3	9	27	81	243

c. Given only the number of users in 2005 and the assumption that the number of users triples each year, how did you determine the number of users for years 2, 3, 4, and 5?

I MULTIPLIED THE PRECEDING YEAR'S NUMBER OF USERS BY 3.

d. Given only the number of users in 2005 and the assumption that the number of users triples each year, how did you determine the number of users for years 0, -1, -2, and -3?

1 DIVIDED THE NEXT YEARS NUMBER OF USERS BY 3.

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Module 1:



e. Write an equation to represent the number of users in millions, N, for year t, $t \ge -3$.

N= 3t

f. Using the context of the problem, explain whether or not the formula $N=3^t$ would work for finding the number of users in millions in year t, for all $t \le 0$.

WE ONLY KNOW THAT THE NUMBER OF USERS HAS TRIPUED EACH YEAR IN THE TIME FRAME OF 2001 TO 2009. FOR THAT REASON IN ECANNOT RELY ON THE FORMULA, N=3t, TO WORK FOR ALL t=0, JUST TO t=-3, WHICH IS THE YEAR 2001.

g. Assume the total number of users continues to triple each year after 2009. Determine the number of users in 2012. Given that the world population at the end of 2011 was approximately 7 billion, is this assumption reasonable? Explain your reasoning.

2012 IS t=B, 90 WHEN t=B IN N=3t, N=6,561,000,000.

THE NVMBER OF USERS IN 2012, 6,561,000,000 DOES NOT EXCERD) THE WORLD POPULATION OF 7 BILLION, THEREFORE IT IS POSSIBLE TO HAVE THAT NVMBER OF USERS. BUT 6,561,000,000 IS APPROXIMATELY 94% OF THE WORLD'S POPULATION. THE NUMBER OF USERS IS LIKELY LESS THAN THAT DUE TO POVERTY, IUNIESS, INFANCY, ETC. THE ASSUMPTION IS POSSIBLE, BUT NOT REASONABLE.

Module 1:



- Let m be a whole number.
 - Use the properties of exponents to write an equivalent expression that is a product of unique primes, each raised to an integer power.

$$= \frac{(3 \cdot 2)^{21} \cdot 10^{7}}{(3 \cdot 10)^{7}} = \frac{3^{21} \cdot 2^{21} \cdot 10^{7}}{3^{7} \cdot 10^{7}}$$

$$= 3^{21-7} \cdot 2^{21} \cdot 10^{7-7}$$

$$= 3^{14} \cdot 2^{21} \cdot 10^{9}$$

$$= 3^{14} \cdot 2^{21}$$

Use the properties of exponents to prove the following identity:

$$\frac{6^{3m} \cdot 10^m}{30^m} = 2^{3m} \cdot 3^{2m}$$

$$\frac{6^{3m} \cdot 10^{m}}{30^{m}} = \frac{(3 \cdot 2)^{3m} \cdot 10^{m}}{(3 \cdot 10)^{m}}$$

$$= \frac{3^{3m} \cdot 2^{3m} \cdot 10^{m}}{3^{m} \cdot 10^{m}}$$

$$= 3^{3m-m} \cdot 2^{3m} \cdot 10^{m-m} = 3^{2m} \cdot 2^{3m} = 2^{3m} \cdot 3^{2m}$$

What value of m could be substituted into the identity in part (b) to find the answer to part (a)?

$$2^{3m} \cdot 3^{2m} = 2^{21} \cdot 3^{14}$$
 $3m = 21$
 $m = 7$
 $m = 7$
THEREFORE, $m = 7$.



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3.

a. Jill writes $2^3 \cdot 4^3 = 8^6$ and the teacher marked it wrong. Explain Jill's error.

JILL MULTIPLIED THE BASES, 2 AND 4, AND ADDED THE EXPONENTS. YOU CAN ONLY ADD THE EXPONENTS WHEN THE BASES BEING MULTIPLIED ARE THE SAME.

Find n so that the number sentence below is true:

$$4^{3} = 4.4.4$$

 $= (2.2)(2.2)(2.2)$
 $= 2^{3}.4^{3} = 2^{3}.2^{6} = 2^{9}$
 $= 2^{6}$
 $= 2^{6}$
 $= 2^{6}$
 $= 2^{6}$
 $= 2^{6}$

 $2^3 \cdot 4^3 = 2^3 \cdot 2^n = 2^9$

Use the definition of exponential notation to demonstrate why $2^3 \cdot 4^3 = 2^9$ is true.

 $4^{3}=2^{6}$, so $2^{3}\cdot 4^{3}=2^{9}$ is Equivalent to $2^{3}\cdot 2^{6}=2^{9}$. By DEFINITION OF EXPONENTIAL NOTATION: $2^{3}\cdot 2^{6}=(2\times \times 2)\times (2\times \times 2)=(2\times \times 2)=2^{3+6}=2^{9}$

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Module 1:

d. You write $7^5 \cdot 7^{-9} = 7^{-4}$. Keisha challenges you, "Prove it!" Show directly why your answer is correct without referencing the laws of exponents for integers; in other words, $x^a \cdot x^b = x^{a+b}$ for positive numbers x and integers a and b.

$$\eta_5.\eta^{-9} = \eta_5. \frac{1}{\eta_9}$$
 By Definition

$$= \frac{\eta_5}{\eta_9}$$
 By PRODUCT FORMULA

$$= \frac{\eta_5}{\eta_9}$$
 By $\chi^m.\chi^n = \chi^{m+n}$ for $\chi > 0$, $m,n \ge 0$

$$= \frac{1}{\eta_9}$$
 By EQUIVARIANT FRACTIONS

$$= \eta_9$$
 By DEFINITION.

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